

Second Edition
**Field and Wave
Electromagnetics**

David K. Cheng



FIELD AND WAVE ELECTROMAGNETICS

DAVID K. CHENG
SYRACUSE UNIVERSITY



ADDISON-WESLEY PUBLISHING COMPANY

Reading, Massachusetts Menlo Park, California
London Amsterdam Don Mills, Ontario Sydney

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