



OPTIONS,
FUTURES,
AND OTHER
DERIVATIVES

SEVENTH EDITION

JOHN C. HULL

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AND OTHER DERIVATIVES**



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